

# THE USE OF THE SOFTWARE MATLAB TO IMPROVE CHEMICAL ENGINEERING EDUCATION

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**ABSTRACT** - In all the Brazilian Universities involved with the project "Prodenge – Reenge", the main objective is to improve teaching and learning procedure for engineering disciplines. The Chemical Engineering College of Campinas State University focused its effort on the use of engineering softwares. The work developed by this project has allowed all Chemical Engineering undergraduates to deal with commercial softwares which make engineering calculations and estimates easier. The following work aims Chemical Engineering Process Simulation and Control improvement through the use of the commercial software MATLAB.

The main concern is to develop some useful case studies which are able to bring out the important characteristics for the control structure design and implementation. Beyond the process simulation and control application, the user has the main concepts related to control theory readily available in an interactive fashion.

The present work has been divided in two parts. The first one consists of Process Control fundamental theory so that an undergraduate can either review or have a first contact with the subject. The second part of the work is an ideal binary distillation column study where some important aspects of the control theory have been implemented.

## Part One

The first part consists of some important process control definitions. Some of them are presented below.

### Types of variables

The process variables can be divided in 3 groups: manipulated variables, controlled variables and load variables.

- Manipulated variables

They are independent variables which are entering or leaving the process and can be changed to make the control.

- Controlled variables

They are the variables in which the control will be made. This control can be made either maintaining these variables as constant as possible or making them follow a desired trajectory.

Example: Temperature inside a reactor.

- Load variables

It is not possible to manipulate with these variables. Although the effects of the load variables, the control system must be prepared to work perfectly.

### What is a controller ?

The construction and operation details of a controller change from manufacturer to manufacturer, but its basic functioning is the same.

All controller aims to compare the signal which comes from the transmitter with the set-point and sends a signal to the control valve. The way that the controller compares the process signal with the set point depends on the type of action wanted. Basically there are 3 kinds of actions in a feedback controller: proportional action, integral action and derivative action.

### Proportional controller (P)

The output signal is compared to the set-point and is changed proportionally to the input signal error. A

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proportional controller just acts when an error is measured. The equation of this type of controller is:

$$m(t) = \bar{m} + K_c (C_{sp} - C) \quad (1)$$

where:

$m(t)$  = controller output signal which adjusts the control valve

$\bar{m}(t)$  = controller output signal when the error is zero

$K_c$  = controller gain

$C$  = process signal from transmitter

$C_{sp}$  = set-point signal (process desired signal)

$C - C_{sp}$  = error ( $e(t)$ )

$$m(t) = \bar{m} + \frac{1}{I} \int e(t) dt$$

(2)

where:

$I$  = integral time

### Proportional Integral Derivative Controller (PID)

All of the three actions (proportional, integral and derivative) are included. The derivative action is an anticipative action where the controller aims to anticipate the future system characteristic based on the derivative of the error (the time rate of change of the error). This action is quick and is always in the opposite direction of the error occurred in the system. The equation of a proportional integral controller is:

$$m = \bar{m} + K_c \left[ e + \frac{1}{I} \int e dt + K_D \frac{de}{dt} \right]$$

(3)

where:

$K_D$  = derivative time

### Control Strategies

There are many control strategies. Some of them are presented below.

#### Feedback Control

The variable wanted to be controlled is measured and compared to a desired value (the set-point). The error between the process variable and the set-point is turned into an input so that the controller can act in the system. Therefore, the controller does not make any action until an error in the system is detected. It is an action to bring the system back to the set-point.

#### Feedforward Control

The variable is measured and a corrective action is taken before it upset the process. It is basically an action to maintain the system in the set-point. The

### Proportional Integral Controller (PI)

An integral controller has a proportional plus an integral action. In an integral action the control valve moves based on the time integral of the error. This action aims to bring back the system to the set-point and also avoids it to go away from the set point. One important characteristic of such controller is that, due to the integral action, the response can be very slow. The equation of this type of controller is:

great advantage of this strategy is that it allows, theoretically, a perfect control. However, in many applications this is not feasible.

### Feedforward / Feedback control

Feedforward control is often used in combination with feedback control. Each type of control compensates the disadvantages of the other one.

### Ratio control

This is a special type of feedback control. The objective is not to control the performance of two independent variables  $M$ ,  $L$  but to control the ratio  $R_a$ :

$$R_a = \frac{M}{L} \quad (4)$$

Some applications of ratio control are, for instance, the control of a specific reflux ratio for a distillation column or the holding of a fuel air ratio to a furnace at an optimum value.

### Part Two

The second part of this work is an ideal binary distillation column study. Several additional assumptions and idealizations were made. These hypothesis are sometimes valid but they are frequently only crude approximations. However, the purpose of studying this simplified model case is to reduce the problem to its most elementary form so that the basic structure of the equations can be clearly seen.

First of all, the column was modeled considering equimolar overflow (whenever a mole of vapor condenses, it vaporizes a mole of liquid), which eliminates an energy equation for each tray. The holdup of vapor is assumed negligible and a simple linear relationship between the liquid holdup, ( $M_N$ ) and the liquid flow rate leaving the tray,  $L_N$  is also considered. A further assumption made is a pure binary system with constant molar relative volatility

through the column and perfect 100 percent efficient trays. The variables used to model the column are presented below:

$N_s$  = feed tray of the column  
 $F$  = feed rate (moles/s)  
 $x_F$  = composition of liquid in the feed tray  
 $M_D$  = holdup of liquid in the reflux drum (moles)  
 $x_D$  = composition of the liquid in the drum  
 $N_T$  = top tray of the column  
 $y_{NT}$  = composition of vapor in the top of the column  
 $R$  = rate of reflux (moles/s)  
 $D$  = rate of overhead distillate product removed (moles/s)  
 $B$  = rate of liquid bottoms product removed (moles/s)  
 $x_B$  = liquid composition in the base of the column  
 $V$  = rate of vapor generated in the reboiler of the column (moles/s)  
 $M_B$  = holdup in the reboiler (moles)  
 $M_N$  = holdup on each tray (moles)  
 $x_N$  = composition of liquid in each tray  
 $y_N$  = composition of vapor in each tray  
 $\beta$  = hydraulic constant of the trays  
 $R_0$  = initial reflux rate  
 $\bar{M}_N$  = constant

There are 4 equations per tray: a total and a component continuity, a liquid hydraulic equation and a vapor-liquid equilibrium equation. These equations are presented below.

Vapor-liquid equilibrium equation:

$$y_n = \frac{\beta x_n}{1 + (\beta - 1)x_n} \quad (5)$$

Liquid hydraulic equation:

$$L_N = \bar{L}_N + \frac{M_N - \bar{M}_N}{\beta} \quad (6)$$

Total continuity:

$$\frac{d(M_N)}{dt} = L_{N+1} - L_N \quad (7)$$

Component continuity:

$$\frac{d(M_N x_N)}{dt} = L_{N+1} x_{N+1} - L_N x_N + V y_{N-1} - V y_N \quad (8)$$

A feedback control was made through 2 controllers PI which change the reflux  $R$  and the vapor  $V$  to control overhead distillate composition  $x_D$  and bottom composition  $x_B$ . The equations for each controller are:

$$V = V_0 - K_{c_B} \text{err}_B + \frac{1}{I_B} \text{err}_B \int dt \quad (9)$$

where:

$$\text{err}_B = x_{B \text{ set-point}} - x_B$$

$$R = R_0 + K_{c_D} \text{err}_D + \frac{1}{I_D} \text{err}_D \int dt \quad (10)$$

where:

$$\text{err}_D = x_{D \text{ set-point}} - x_D$$

The initial conditions given for the column are:

$$\begin{aligned}
 N_T &= 20 \\
 x_{D \text{ set-point}} &= 0.98 \\
 x_{B \text{ set-point}} &= 0.02 \\
 x_{F \text{ set-point}} &= 0.5 \\
 N_F &= 10 \\
 M_{D0} &= 100 \text{ moles} \\
 M_{B0} &= 100 \text{ moles} \\
 M_0 &= 10 \text{ moles} \\
 R_0 &= 128.01 \text{ moles/s} \\
 V_0 &= 178.01 \text{ moles/s} \\
 F &= 100 \text{ moles/s} \\
 &= 0.1 \\
 &= 2
 \end{aligned}$$

The constants of the 2 controller are:

$$\begin{aligned}
 K_{c_D} &= 1000 \\
 K_{c_B} &= 1000 \\
 I_D &= 5 \\
 I_B &= 1.25
 \end{aligned}$$

To make the control of the given column, a program was made in the software MATLAB. The program asks the student a perturbation in the composition of the feed stream. The program is listed below:

```

% initial variables
NT=20;NF=10;MDO=100;MBO=100;MO=10;
RO=128.01;VO=178.01;F=100;BETA=0.1;
ALFA=2;
% CONTROLLER CONSTANTS
KCD=1000;KCB=1000;
TAUD=5;TAUB=1.25;
ERINTB=0;ERINTD=0;
% Perturbation
Z=input('Enter with a perturbation between 0 and 1
Z=');
% INITIAL VALUES OF X
XB=0.02;
X=[0.035 0.05719 0.08885 0.1318 0.18622 0.24951
0.31618 0.37948 0.43391 0.47688 ...
0.51526 0.56295 0.61896 0.68052 0.74345 0.80319
0.85603 0.89995 0.93458 0.96079];
XD=0.98;
% initial conditions
for N=1:NT
M(N)=MO;
MX(N)=M(N)*X(1,N);
LO(N)=RO+F;
if N>NF
LO(N)=RO;
end;
end;
Time=0;DELTA=0.005;ERINTD=0;ERINTB=0;i=1
;
while Time<12
% LIQUID HYDRAULIC EQUATION AND VLE
for N=1:20
Y(N)=ALFA*X(1,N)/(1+(ALFA-1)*X(1,N));
L(N)=LO(N)+(M(N)-MO)/BETA;
end;
YB=ALFA*XB/(1+(ALFA-1)*XB);

```

```

% 2 CONTROLLERS FEEDBACK PI
ERRB=0.02-XB;
ERRD=0.98-XD;
V=VO-KCB*(ERRB+ERINTB/TAUB);
R=RO+KCD*(ERRD+ERINTD/TAUD);
D=V-R;
B=L(1)-V;
if R<0 disp('level too low or unreal composition ')
end;
if V<0 disp('level too low or unreal composition ')
end;
if D<0 disp('level too low or unreal composition ')
end;
if B<0 disp('level too low or unreal composition')
end;
% CÁLCULATION OF DERIVATIVES
XBDOT=(L(1)*X(1,1)-V*YB-B*XB)/MBO;
MDOT(1)=L(2)-L(1);
MXDOT(1)=V*(YB-Y(1))+L(2)*X(1,2)-L(1)*X(1,1);
for N=2:NF-1
MDOT(N)=L(N+1)-L(N);
MXDOT(N)=V*(Y(N-1)-Y(N))+L(N+1)*X(1,N+1)-
L(N)*X(1,N);
end;
% FEED TRAY
MDOT(NF)=L(NF+1)-L(NF)+F;
MXDOT(NF)=V*(Y(NF-1)-
Y(NF))+L(NF+1)*X(1,NF+1)-L(NF)*X(1,NF)+F*Z;
for N=(NF+1):(NT-1)
MDOT(N)=L(N+1)-L(N);
MXDOT(N)=V*(Y(N-1)-Y(N))+L(N+1)*X(1,N+1)-
L(N)*X(1,N);
end;
MDOT(NT)=R-L(NT);
MXDOT(NT)=V*(Y(NT-1)-Y(NT))+R*X(1,NT)-
L(NT)*X(1,NT);
XDDOT=V*(Y(NT)-XD)/MDO;
% Euler Integration
Time=Time+DELTA;
XB=XB+DELTA*XBDOT;
for N=1:NT
M(N)=M(N)+MDOT(N)*DELTA;
MX(N)=MX(N)+MXDOT(N)*DELTA;
X(1,N)=MX(N)/M(N);
end;
XD=XD+XDDOT*DELTA;
ERINTD=ERINTD+ERRD*DELTA;
ERINTB=ERINTB+ERRB*DELTA;
A(i,:)=[ Time XB X(1,10) XD R V];
i=i+1;
end;
figure(1);plot(A(:,1),A(:,2),'c-'),xlabel('Time
[hr]'),ylabel('XB');grid;
figure(2);plot(A(:,1),A(:,3),'r-'),xlabel('Time
[hr]'),ylabel('XF');grid;
figure(3);plot(A(:,1),A(:,4),'g-'),xlabel('Time
[hr]'),ylabel('XD');grid;
figure(4);plot(A(:,1),A(:,5),'b-'),xlabel('Time
[hr]'),ylabel('R (moles/hr)');grid;
figure(5);plot(A(:,1),A(:,6),'m-'),xlabel('Time
[hr]'),ylabel('rate of vapor (moles/hr)');grid;
For a step perturbation in the composition of the feed
stream from 0.5 to 0.55, the program gives the
following graphics:

```

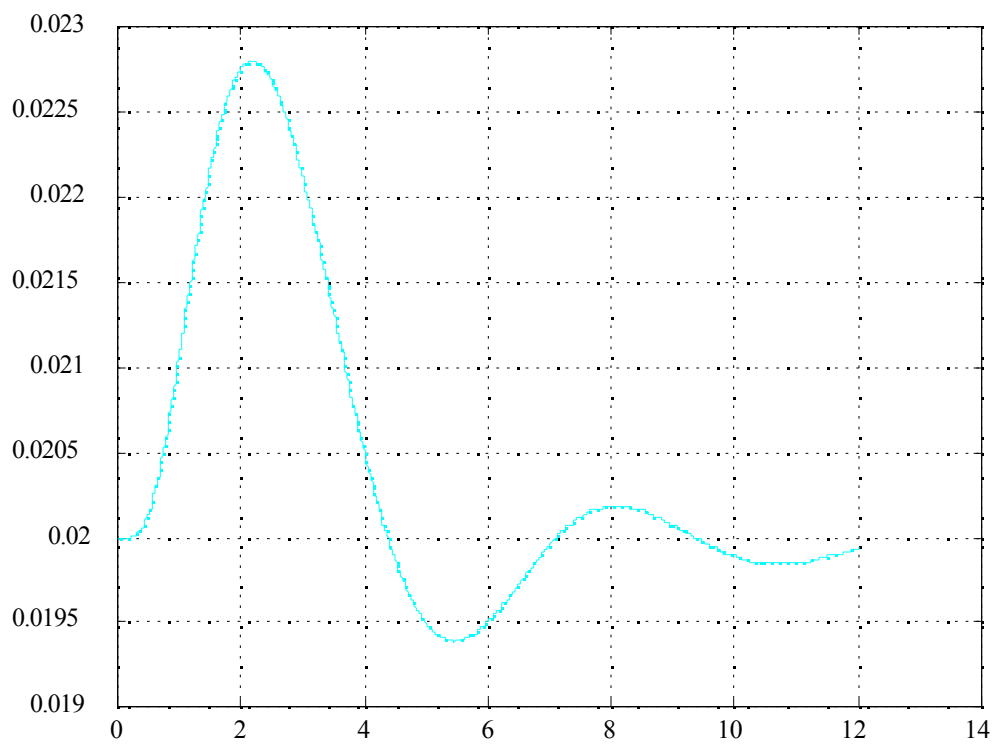


Figure 1. Graphic of composition  $x_B$  X time (hours)

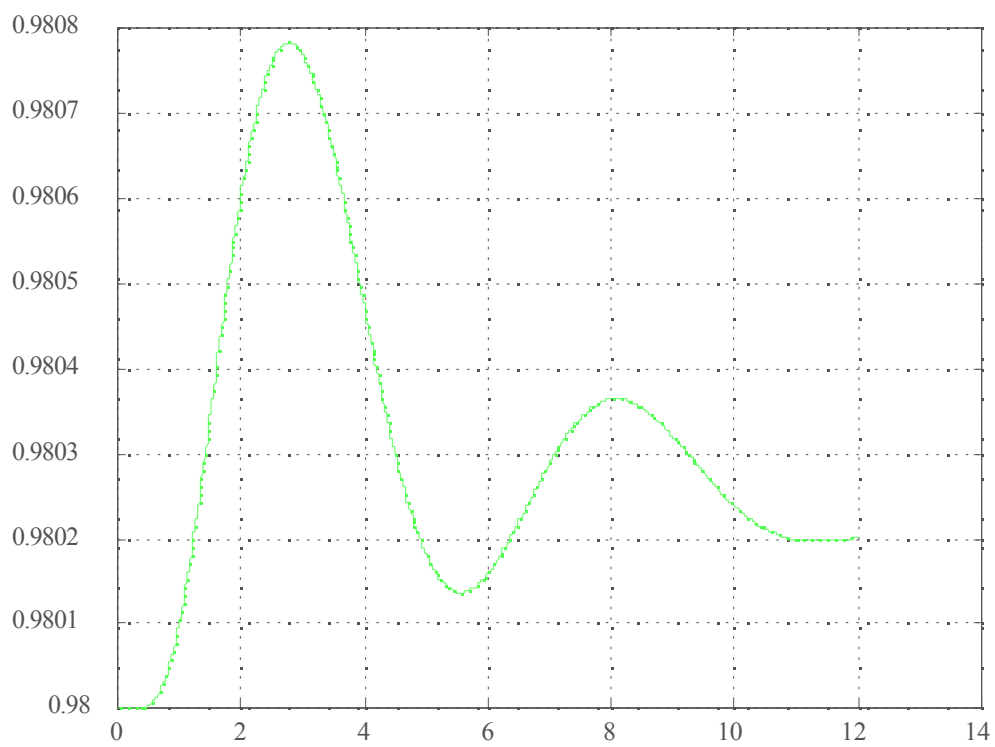


Figure 2. Graphic of composition  $x_D$  X time (hours)

Observing the graphics it can be seen that, after the perturbation, the control acts in the system and the compositions stabilize.

### **Other activities**

All of the present work will be accessible to all Chemical Engineering undergraduates of UNICAMP through home-pages to create a deep interaction between the students and the studied subjects.

Moreover, 2 performances regarding this work were made to all professors of Chemical Engineering College of UNICAMP. In both lectures the participation of all professors in the project "Prodenge-

output

Reenge" was encouraged as well as the undergraduates' contribution.

### **References**

- 1) Luyben, W.L; "Process Modeling, Simulation and Control for Chemical Engineers"; 2<sup>nd</sup> Edition; Mc Graw-Hill, 1974.
- 2) Seborg, Dale E., Thomas F. Edgar and Duncan A. Mellichamp; "Process Dynamics and Control"; 1<sup>st</sup> Edition; John Wiley and Sons, 1989.